## 3

## Area of a Triangle

1. In the figure below, XYZ is a triangle.


When XZ is the base, what is the height of Triangle XYZ?
(1) DY
(2) EZ
(3) $X Y$
(4) YZ
2. In the figure below, ABC is a triangle.


Given that EC is the height, what is the base of Triangle ABC?
(1) AB
(2) AC
(3) AD
(4) AE
3. In the figure below, XYZ is a triangle.


Given that XY is the base, what is the height of Triangle XYZ?
(1) AY
(2) CX
(3) BZ
(4) YZ
4. In the figure below, PRS is a triangle.


Which of the following pairs shows the correct base and its corresponding height for finding the area of Triangle PRS?
Base Height
(1) TR PT
(2) $\mathrm{SR} \quad \mathrm{PS}$
(3) PQ SQ
(4) PR $\quad \mathrm{QS}$
5. The figure below shows a rectangle ABDF.


Which one of the following pairs of triangles has the same height?
(1) Triangle ABC and Triangle EFG
(2) Triangle AEF and Triangle CAG
(3) Triangle CAB and Triangle AGF
(4) Triangle CAF and Triangle CDF
6. Find the shaded area in the figure below.

(1) $17 \mathrm{~cm}^{2}$
(2) $21 \mathrm{~cm}^{2}$
(3) $38 \mathrm{~cm}^{2}$
(4) $42 \mathrm{~cm}^{2}$
7. In the figure below, $A B C D$ is a rectangle and $C E F G$ is a square.


Find the area of Triangle ABG.
(1) $9 \mathrm{~cm}^{2}$
(2) $24 \mathrm{~cm}^{2}$
(3) $33 \mathrm{~cm}^{2}$
(4) $48 \mathrm{~cm}^{2}$
8. In the figure below, $D E F G$ is a rectangle and $G X=X F$.


What is the ratio of the area of Triangle DGX to the area of Triangle DGE?
(1) $1: 2$
(2) $1: 3$
(3) $2: 1$
(4) $3: 1$
9. The figure ABCD is made up of 6 identical rectangles. ACE is a triangle.


What fraction of the figure $A B C D$ is shaded?
(1)

$$
\frac{1}{12}
$$

(2)
$\frac{1}{6}$
(3)
$\frac{1}{2}$
(4) $\frac{1}{3}$
10. The figure below shows a rectangle $A B C D$.


Which of the following triangles has an area that is half of Rectangle ABCD?
(1) BCF
(2) BCH
(3) CFG
(4) ECG
11. The figures below show 4 identical rectangles.


A


B


C


D

Which two of the shaded figures have the same area?
(1) A and B
(2) A and C
(3) $B$ and $D$
(4) C and D
12. The figure below shows a triangle with a shaded region.


Find the area of the shaded region.
(1) $12 \mathrm{~cm}^{2}$
(2) $36 \mathrm{~cm}^{2}$
(3) $42 \mathrm{~cm}^{2}$
(4) $84 \mathrm{~cm}^{2}$
13. The figure below shows Rectangle $\mathrm{ABCD} . \mathrm{AB}$ is $8 \mathrm{~cm}, \mathrm{AD}$ is 6 cm and BD is 10 cm . EF is 2 cm and is perpendicular to $B D$.


Find the shaded area.
(1) $12 \mathrm{~cm}^{2}$
(2) $14 \mathrm{~cm}^{2}$
(3) $24 \mathrm{~cm}^{2}$
(4) $38 \mathrm{~cm}^{2}$
14. The figure below shows Triangle ACF and Rectangles ADFE and EFCB.


Who made a correct statement about the area of Triangle ACF?
Nadia: The area of Triangle ACF is the same as the area of Rectangle ABCD.
Jeremy: The area of Triangle ACF is half the area of Rectangle ABCD.
Amanda: The area of Triangle ACF is the same as the area of Rectangle EFCB.
Bernard: The area of Triangle ACF is half the area of Rectangle EFCB.
(1) Nadia
(2) Jeremy
(3) Amanda
(4) Bernard
15. The figure below shows Rectangle $A B C D$. $F$ is the mid-point of $A C$ and $E$ is the mid-point of $A F$.


If the total shaded area is $120 \mathrm{~cm}^{2}$, find the area of Rectangle ABCD .
(1) $240 \mathrm{~cm}^{2}$
(2) $300 \mathrm{~cm}^{2}$
(3) $360 \mathrm{~cm}^{2}$
(4) $480 \mathrm{~cm}^{2}$
16. The figure below is made up of 8 identical squares. What fraction of the figure is shaded? Express your answer in its simplest form.


Ans: $\qquad$
17. Find the area of the shaded triangle in the square grid below.


Ans: $\qquad$ $\mathrm{cm}^{2}$
18. Find the area of the shaded region below.

$\qquad$ $\mathrm{cm}^{2}$
19. Name the height of Triangle BCF.


Ans: $\qquad$
20. In the figure below, WXYZ is a square and WYZ is a triangle. The perimeter of WXYZ is 128 cm . Find the area of Triangle WYZ.


Ans: $\qquad$ $\mathrm{cm}^{2}$
21. The figure below is made up of Triangle ABC and Triangle ACD. Find the area of Triangle ACD.


Ans:
$\mathrm{cm}^{2}$
22. In the figure below, $A B C D$ is a rectangle and $B M=M C$. Express the area of the shaded part to the area of the unshaded part as a ratio in the simplest form.


Ans: $\qquad$
23. ABCD is a rectangle. $\mathrm{AB}=42 \mathrm{~cm}$ and $\mathrm{BC}=17 \mathrm{~cm}$. The ratio of the length of DE to the length of EC is $2: 1$. What is the area of Triangle DBE?


Ans: $\qquad$ $\mathrm{cm}^{2}$
24. $A B C D$ is a rectangle. The perimeter of $A B C D$ is 34 cm . The length of $D E$ is 6 cm . The length of $B C$ is 8 cm . Find the area of the shaded part.


Ans: $\qquad$ $\mathrm{cm}^{2}$
25. $\mathrm{W}, \mathrm{X}, \mathrm{Y}$ and Z are the mid-points of the sides of a square ABCD . The area of the square is $64 \mathrm{~cm}^{2}$. What is the area of the shaded triangle?


Ans: $\qquad$ $\mathrm{cm}^{2}$
26. In the figure below, KLMN and NRQP are squares. The length of KN is 5 cm and the length of NP is 13 cm . Find the total area of the shaded parts.


Ans: $\qquad$ $\mathrm{cm}^{2}$
27. The figure below shows two identical triangles with an overlapped area. Given that the overlapped area is $32 \mathrm{~cm}^{2}$, find the area of the whole figure.

$\qquad$
28. Find the area of the shaded triangle.


Ans: $\qquad$ $\mathrm{cm}^{2}$
29. The area of Triangle ACE is $75 \mathrm{~cm}^{2}$. The area of Square BDEF is $36 \mathrm{~cm}^{2}$. The length of AE is 15 cm . Find the shaded area.


Ans: $\qquad$ $\mathrm{cm}^{2}$
30. ABCD is a square. The length of BC is 20 cm and the length of FG is 6 cm . Find the shaded area.


Ans: $\qquad$ $\mathrm{cm}^{2}$
31. The figure below is made up of 2 squares. The length of $C E$ is 36 cm and $D E$ is twice as long as CD. Find the area of Triangle ACE.

Ans: $\qquad$ $\mathrm{cm}^{2}$
32. In the figure below, ABCD is a rectangle and the area of Triangle EFG is $30 \mathrm{~cm}^{2}$. AE is $\frac{1}{2}$ of AD . Find the length of AD .


Ans: $\qquad$ cm
33. The figure below is made up of Triangle ABC, Triangle ABD and 2 identical rectangles. The area of Triangle $A B C$ is $36 \mathrm{~cm}^{2}$. What is the area of Triangle ABD?


Ans: $\qquad$ $\mathrm{cm}^{2}$
34. ABCD and DEFG are rectangles. The area of Triangle $C D F$ is $24 \mathrm{~cm}^{2}$ and $A G=G D$. Find the area of Rectangle ABCD.


Ans: $\qquad$ $\mathrm{cm}^{2}$
35. $P Q R S$ is a rhombus of sides 13 cm . Points $T$ and $U$ are the mid-points of lines $P Q$ and $S R$ respectively. The length of QV is 12 cm . Find the area of the shaded region.


Ans: $\qquad$ $\mathrm{cm}^{2}$
36. The figure $A B C D E F$ is made up of two triangles ADF and CDE. The area of the shaded triangle BDE is $96 \mathrm{~cm}^{2}$, which is half of the area of Triangle CDE. $\mathrm{FE}=\mathrm{ED}=14 \mathrm{~cm}$. What is the total area of the figure ABCDEF?


Ans: $\qquad$ $\mathrm{cm}^{2}$
37. In the figure below, $U V X Z$ and $V W Y Z$ are rectangles. $V U=9 \mathrm{~cm}, U Z=12 \mathrm{~cm}$ and $V Z=15 \mathrm{~cm}$. Find the length of YZ.


Ans: $\qquad$ cm
38. In the figure below, the rectangle is divided into 4 triangles. The areas of Triangles $\mathrm{A}, \mathrm{B}$ and C are $300 \mathrm{~cm}^{2}, 225 \mathrm{~cm}^{2}$ and $100 \mathrm{~cm}^{2}$ respectively. Find the area of Triangle D.


Ans: $\qquad$ $\mathrm{cm}^{2}$
39. The area of Rectangle $A B C D$ is $560 \mathrm{~cm}^{2}$. The area of Triangle CDF is $160 \mathrm{~cm}^{2}$. Find the area of the shaded triangle DEF.


Ans: $\qquad$ $\mathrm{cm}^{2}$
40. The figure below is made up of Square ABGH and Rectangle CDEG. Each side of Square ABGH is $8 \mathrm{~cm} . \mathrm{BC}=1 \mathrm{~cm}, \mathrm{CD}=10 \mathrm{~cm}$ and $\mathrm{FE}=4 \mathrm{~cm} . \mathrm{HMD}$ and HGFE are straight lines. Find the total area of the shaded parts.


Ans: $\qquad$ $\mathrm{cm}^{2}$
41. The figure below shows a rectangle $A B C D$. $E G$ is a straight line parallel to $A B$. $A D$ is thrice of $A E$. The area of Triangle CDF is $32 \mathrm{~cm}^{2}$. Find the shaded area.


Ans: $\qquad$ $\mathrm{cm}^{2}$
42. The figure below is made up of Rectangle ABCD and 2 overlapping triangles BEC and BFC . The total area of the shaded parts is $150 \mathrm{~cm}^{2}$. If the area of Rectangle $A B C D$ is $600 \mathrm{~cm}^{2}$, find the area of the unshaded part X.


Ans: $\qquad$ $\mathrm{cm}^{2}$
43. The figure below is made up of triangles. PR is a straight line.


Each statement below is either true, false or not possible to tell from the information given. For each statement, put a tick $(\sqrt{ })$ in the correct column.

| Statement | True | False | Not possible to tell |
| :---: | :---: | :---: | :---: |
| The line QS can be the height of both <br> Triangle QRS and Triangle PQS. |  |  |  |
| If the base of Triangle PQR is PR, <br> the height is PQ. |  |  |  |

44. Study the figure below and answer the following questions.
(a) DE is the height of Triangle ACE. Name the line that represents the base of the same triangle.
(b) AE is the base of Triangle ACE. Name the line that represents the height of the same triangle.


Ans: (a) $\qquad$
(b) $\qquad$
45. Triangle ABC is shown below.


Each statement below is either true, false or not possible to tell from the information given. For each statement, put a tick $(\sqrt{ })$ in the correct column.

| Statement | True | False | Not possible to tell |
| :---: | :---: | :---: | :---: |
| The area of Triangle ABC is $90 \mathrm{~cm}^{2}$. |  |  |  |
| When the height and base of Triangle <br> ABC is doubled, the area of the new <br> triangle is also doubled. |  |  |  |

46. Triangle ABD is made up of Triangle ABE, Triangle BEC and Triangle CED. The area of Triangle BED is $16 \mathrm{~cm}^{2}$.
(a) What is the area of Triangle ABE?
(b) What is the area of Triangle EBC?


Ans: (a) $\qquad$ $\mathrm{cm}^{2}$
(b) $\qquad$ $\mathrm{cm}^{2}$
47. In the figure below, Rectangle ABCD is made up of 8 smaller identical rectangles. Given that $A B=24 \mathrm{~cm}$, what is the area of Triangle ACY?


Ans: $\qquad$ $\mathrm{cm}^{2}$
48. $A B C D$ is a rectangle and $P Q R$ is a triangle with $R C=C Q$. Find the area of the figure ASPQD.


Ans:
$\mathrm{cm}^{2}$
49. In the figure below, $A B C D$ is a square and EFG is a triangle. $\frac{1}{8}$ of the square is shaded. Find the unshaded area of Triangle EFG.


Ans: $\qquad$ $\mathrm{cm}^{2}$
50. The figure below is made up of two squares and two triangles. The area of Square BCDE is $25 \mathrm{~cm}^{2}$, the area of Square EFGH is $169 \mathrm{~cm}^{2}$ and the area of the isosceles triangle ABH is $72 \mathrm{~cm}^{2} . \mathrm{AB}=\mathrm{BH} . \mathrm{ABE}$ and HBC are straight lines.
(a) Find the area of Triangle BHE.
(b) Find the perimeter of the shaded area.


Ans: (a) $\qquad$ $\mathrm{cm}^{2}$
(b) $\qquad$ cm
51. In the figure below, ABCD is a rectangle. AFC and BFE are straight lines. The area of Triangle CEF is $130 \mathrm{~cm}^{2}$. The length of EC is half the length of DE. What is the total area of the shaded region?


Ans: $\qquad$ $\mathrm{cm}^{2}$
52. In the figure below, $A B C D$ is a rectangle. The length of the rectangle is twice its breadth. The ratio of the length of AP to the length of AD is $3: 7$.
(a) Find the length of AD.
(b) Find the area of the shaded region.


Ans: (a) $\qquad$ cm
(b) $\qquad$ $\mathrm{cm}^{2}$
53. Figure 1 is a right-angled triangle with one of the sides as 4 cm . Figure 2 is made up of 4 such right-angled triangles and a square. Find the area of Figure 2.


Figure 1


Ans: $\qquad$ $\mathrm{cm}^{2}$
54. In the figure below, there are 3 squares of sides $7 \mathrm{~cm}, 9 \mathrm{~cm}$ and $4 \mathrm{~cm} . \mathrm{AB}$ and CD are straight lines. Find the shaded area.


Ans: $\qquad$ $\mathrm{cm}^{2}$

## 3 <br> Area of a Triangle

## Solution 1

## 1

The height of a triangle is perpendicular to its base. DY is perpendicular to XZ.


## Solution 2

## 1

The height of a triangle is perpendicular to its base. AB extended is perpendicular to EC.


## Solution 3

## 3

The height of a triangle is perpendicular to its base. BZ is perpendicular to XY extended.


## Solution 4

## 4

Option 1:
Incorrect. Base TR and height PT are used for finding the area of Triangle PRT.

Option 2:
Incorrect. PS is not perpendicular to SR.
Option 3:
Incorrect. Base PQ and height SQ are used for finding the area of Triangle PQS.

## Solution 5

4
For Triangle CAF, the height is FD and the base is AF.

For Triangle CDF, the height is FD and the base is CD.

## Solution 6

1

Area of the whole triangle $=\frac{1}{2} \times 6 \times 7$
$=21 \mathrm{~cm}^{2}$

Area of the shaded figure $=21-4=17 \mathrm{~cm}^{2}$

## Solution 7

2
Area of Triangle ABG $=\frac{1}{2} \times 8 \times 6=24 \mathrm{~cm}^{2}$

## Solution 8

1
Area of Triangle $\mathrm{DGX}=\frac{1}{2} \times \mathrm{DG} \times \mathrm{GX}$
Area of Triangle DGE $=\frac{1}{2} \times D G \times D E$
$=\frac{1}{2} \times \mathrm{DG} \times(2 \times \mathrm{GX})=\mathrm{DG} \times \mathrm{GX}$
Area of Triangle DGX : Area of Triangle DGE $=1: 2$

## Solution 9

## 2

Area of Triangle $\mathrm{ACE}=\frac{1}{2} \times \mathrm{CD} \times \mathrm{AE}$
$=\frac{1}{2} \times \mathrm{CD} \times\left(\frac{2}{6} \times \mathrm{AD}\right)=\frac{1}{6} \times \mathrm{CD} \times \mathrm{AD}$
$=\frac{1}{6} \times$ Area of ABCD

## Solution 10

1
For Triangle $B C F$, the height is $A B$ and the base is BC.

Area of Triangle $B C F=\frac{1}{2} \times A B \times B C$
$=\frac{1}{2} \times$ Area of Rectangle ABCD

## Solution 11

2

Shaded area of Figure A
$=$ Shaded area of Figure C
$=\frac{1}{2} \times$ Length of rectangle
$\times$ Breadth of rectangle

## Solution 12

1


Area of Region $A$ and $B=\frac{1}{2} \times(6+2) \times 12$
$=48 \mathrm{~cm}^{2}$

Area of Region $\mathrm{A}=\frac{1}{2} \times 6 \times 12=36 \mathrm{~cm}^{2}$
Area of shaded region $=48-36=12 \mathrm{~cm}^{2}$

## Solution 13

2
Area of Rectangle $\mathrm{ABCD}=8 \times 6=48 \mathrm{~cm}^{2}$

Area of Triangle $\mathrm{ABD}=\frac{1}{2} \times 8 \times 6=24 \mathrm{~cm}^{2}$

Area of Triangle BDE $=\frac{1}{2} \times 10 \times 2=10 \mathrm{~cm}^{2}$
Area of shaded region $=48-24-10$
$=14 \mathrm{~cm}^{2}$

## Solution 14

4

Area of Triangle ACF $=\frac{1}{2} \times \mathrm{FC} \times \mathrm{BC}$
$=\frac{1}{2} \times$ Area of Rectangle EFCB

## Solution 15

4

Considering Triangle ABF only,


Area of Triangle $A B F=\frac{1}{2} \times A B \times 2 h$

Area of Triangle $A B E=\frac{1}{2} \times A B \times h$
Area of Triangle EBF
$=$ Area of Triangle ABE

Considering Triangle ADF only,


Area of Triangle ADF $=\frac{1}{2} \times A D \times 2 h$
Area of Triangle ADE $=\frac{1}{2} \times \mathrm{AD} \times \mathrm{h}$
Area of Triangle ADE
= Area of Triangle DEF
Area of shaded part
$=\frac{1}{2} \times$ Area of Triangle ABD

Area of Rectangle $\mathrm{ABCD}=4 \times 120=480 \mathrm{~cm}^{2}$

## Solution 16

Total area of figure $=8$ units $^{2}$
Area of shaded region $=\frac{1}{2} \times 3 \times 2=3$ units $^{2}$

Fraction of figure which is shaded $=\frac{3}{8}$
Ans: $\frac{3}{8}$

## Solution 17

Area of shaded triangle $=\frac{1}{2} \times 8 \times 4=16 \mathrm{~cm}^{2}$
Ans: $16 \mathrm{~cm}^{2}$

## Solution 18



Area of the whole figure $=9 \mathrm{~cm}^{2}$

Area of Triangle $\mathrm{A}=\frac{1}{2} \times 3 \times 1=1.5 \mathrm{~cm}^{2}$
Area of Triangle $B=\frac{1}{2} \times 2 \times 1=1 \mathrm{~cm}^{2}$

Area of Triangle $\mathrm{C}=\frac{1}{2} \times 3 \times 1=1.5 \mathrm{~cm}^{2}$
Area of the shaded region $=9-1.5-1-1.5$ $=5 \mathrm{~cm}^{2}$

Ans: $5 \mathrm{~cm}^{2}$

## Solution 19

For Triangle BCF, the height is AF and the base is $B C$.

Ans: AF

## Solution 20

Length of a side of the square $=128 \div 4$ $=32 \mathrm{~cm}$

Area of Triangle $\mathrm{WYZ}=\frac{1}{2} \times 32 \times 32=512 \mathrm{~cm}^{2}$
Ans: $512 \mathrm{~cm}^{2}$

## Solution 21

Length of $\mathrm{CD}=\frac{1}{2} \times 20=10 \mathrm{~cm}$
Area of Triangle ACD $=\frac{1}{2} \times 10 \times 15=75 \mathrm{~cm}^{2}$
Ans: $75 \mathrm{~cm}^{2}$

## Solution 22

Area of shaded part $=\frac{1}{2} \times A B \times B M$
$=\frac{1}{2} \times \mathrm{AB} \times\left(\frac{1}{2} \times \mathrm{BC}\right)=\frac{1}{4} \times \mathrm{AB} \times \mathrm{BC}$
$=\frac{1}{4} \times$ Area of Rectangle ABCD
Fraction of rectangle which is unshaded
$=1-\frac{1}{4}=\frac{3}{4}$
Area of shaded part : Area of unshaded part $=1: 3$

Ans: $1: 3$

## Solution 23

Length of $\mathrm{DE}=\frac{2}{3} \times 42=28 \mathrm{~cm}$
Area of Triangle DBE $=\frac{1}{2} \times 28 \times 17=238 \mathrm{~cm}^{2}$
Ans: $238 \mathrm{~cm}^{2}$

## Solution 24

Length of $B C$ and $D C=34 \div 2=17 \mathrm{~cm}$
Length of $E C=17-8-6=3 \mathrm{~cm}$

Area of the shaded part $=\frac{1}{2} \times 8 \times 3=12 \mathrm{~cm}^{2}$
Ans: $12 \mathrm{~cm}^{2}$

## Solution 25



Length of a side of the square $=\sqrt{64}=8 \mathrm{~cm}$

Area of Triangle $P=\frac{1}{2} \times 8 \times 4=16 \mathrm{~cm}^{2}$

Area of Triangle $Q=\frac{1}{2} \times 8 \times 4=16 \mathrm{~cm}^{2}$
Area of Triangle $\mathrm{R}=\frac{1}{2} \times 4 \times 4=8 \mathrm{~cm}^{2}$
Area of the shaded triangle $=64-16-16-8$ $=24 \mathrm{~cm}^{2}$

Ans: $24 \mathrm{~cm}^{2}$

## Solution 26

Area of Square KLMN $=5 \times 5=25 \mathrm{~cm}^{2}$

Area of Triangle NRP $=\frac{1}{2} \times 13 \times 13=84.5 \mathrm{~cm}^{2}$

Area of Triangle LMR $=\frac{1}{2} \times 5 \times(13-5)$
$=20 \mathrm{~cm}^{2}$

Total area of the shaded parts
$=25+84.5+20=129.5 \mathrm{~cm}^{2}$

Ans: $129.5 \mathrm{~cm}^{2}$

## Solution 27

Area of a triangle $=\frac{1}{2} \times 11 \times 14=77 \mathrm{~cm}^{2}$
Area of the whole figure $=(2 \times 77)-32$
$=122 \mathrm{~cm}^{2}$

Note: The overlapped area has to be deducted from the total area of two triangles to avoid double-counting the overlapped area.

Ans: $122 \mathrm{~cm}^{2}$

## Solution 28

Length of the base $=10+7+7=24 \mathrm{~cm}$

Area of the shaded triangle $=\frac{1}{2} \times 24 \times 24$
$=288 \mathrm{~cm}^{2}$

Ans: $288 \mathrm{~cm}^{2}$

## Solution 29

Area of Triangle $\mathrm{ACE}=\frac{1}{2} \times \mathrm{AE} \times \mathrm{CE}$
$75=\frac{1}{2} \times 15 \times \mathrm{CE}$
$\mathrm{CE}=\frac{75 \times 2}{15}=10 \mathrm{~cm}$
Length of a side of Square BDEF $=\sqrt{36}$ $=6 \mathrm{~cm}$

Length of $C D=10-6=4 \mathrm{~cm}$

Shaded area $=\frac{1}{2} \times 4 \times 6=12 \mathrm{~cm}^{2}$

Ans: $12 \mathrm{~cm}^{2}$

## Solution 30

Area of Triangle BEC $=\frac{1}{2} \times 20 \times 20=200 \mathrm{~cm}^{2}$
Area of Triangle $\mathrm{BFC}=\frac{1}{2} \times 20 \times 6=60 \mathrm{~cm}^{2}$

Shaded area $=200-60=140 \mathrm{~cm}^{2}$

Ans: $140 \mathrm{~cm}^{2}$

## Solution 31

Length of $C D=\frac{1}{3} \times 36=12 \mathrm{~cm}$
$\mathrm{AD}=\mathrm{CD}=12 \mathrm{~cm}$

Area of Triangle ACE $=\frac{1}{2} \times 36 \times 12=216 \mathrm{~cm}^{2}$
Ans: $216 \mathrm{~cm}^{2}$

## Solution 32

For Triangle EFG, the height is AE and the base is EG.

Area of Rectangle ABGE $=2 \times 30=60 \mathrm{~cm}^{2}$

Since AE is $\frac{1}{2}$ of AD,
Area of Rectangle $\mathrm{ABCD}=2 \times 60=120 \mathrm{~cm}^{2}$
Length of $A D=120 \div 15=8 \mathrm{~cm}$

Ans: 8 cm

## Solution 33

Triangle ABC and Triangle ABD have the same base AB. The height of Triangle ABC is twice the height of Triangle ABD.

Area of Triangle $\mathrm{ABD}=36 \div 2=18 \mathrm{~cm}^{2}$

Ans: $18 \mathrm{~cm}^{2}$

## Solution 34

Area of Triangle $\mathrm{CDF}=\frac{1}{2} \times \mathrm{CD} \times \mathrm{GD}$
$24=\frac{1}{2} \times \mathrm{CD} \times \mathrm{GD}$
$\mathrm{CD} \times \mathrm{GD}=2 \times 24=48 \mathrm{~cm}^{2}$

Since AG = GD,
Area of Rectangle $\mathrm{ABCD}=2 \times 48=96 \mathrm{~cm}^{2}$

Ans: $96 \mathrm{~cm}^{2}$

## Solution 35

Area of Triangle STR $=\frac{1}{2} \times 13 \times 12=78 \mathrm{~cm}^{2}$
Height of Triangle WSU $=12 \div 2=6 \mathrm{~cm}$
Length of $S U=13 \div 2=6.5 \mathrm{~cm}$
Area of Triangle WSU $=\frac{1}{2} \times 6 \times 6.5=19.5 \mathrm{~cm}^{2}$
Area of shaded region $=78-(2 \times 19.5)$
$=39 \mathrm{~cm}^{2}$
Ans: $39 \mathrm{~cm}^{2}$

## Solution 36

Area of Triangle CBD $=$ Area of Triangle BDE $=96 \mathrm{~cm}^{2}$

Area of Triangle ADF $=\frac{1}{2} \times 20 \times(2 \times 14)$
$=280 \mathrm{~cm}^{2}$

Total area of the figure ABCDEF
$=96+280=376 \mathrm{~cm}^{2}$

Ans: $376 \mathrm{~cm}^{2}$

## Solution 37

Area of Triangle VXZ = Area of Triangle VUZ $=\frac{1}{2} \times 12 \times 9=54 \mathrm{~cm}^{2}$

Area of Triangle $\mathrm{VXZ}=\frac{1}{2} \times \mathrm{VZ} \times \mathrm{YZ}$
$54=\frac{1}{2} \times 15 \times Y Z$
$\mathrm{YZ}=\frac{2 \times 54}{15}=7.2 \mathrm{~cm}$
Ans: 7.2 cm

## Solution 38

Base of Triangle $\mathrm{A}=$ Base of Triangle C
= Length of rectangle
Height of Triangle A + Height of Triangle C
$=$ Breadth of rectangle
$\frac{1}{2} \times$ Area of rectangle
$=$ Area of Triangle A + Area of Triangle C
$=300+100=400 \mathrm{~cm}^{2}$

Area of Triangle $D=400-225=175 \mathrm{~cm}^{2}$

Ans: $175 \mathrm{~cm}^{2}$

## Solution 39

Area of Triangle CDE $=\frac{1}{2} \times 560=280 \mathrm{~cm}^{2}$

Area of shaded triangle $=280-160$
$=120 \mathrm{~cm}^{2}$

Ans: $120 \mathrm{~cm}^{2}$

## Solution 40

Area of Triangle $\mathrm{ABH}=\frac{1}{2} \times 8 \times 8=32 \mathrm{~cm}^{2}$
Length of $\mathrm{HF}=8+10-4=14 \mathrm{~cm}$
Length of $D E=8-1=7 \mathrm{~cm}$

Area of Triangle HDF $=\frac{1}{2} \times 14 \times 7=49 \mathrm{~cm}^{2}$
Total area of shaded parts $=32+49=81 \mathrm{~cm}^{2}$

Ans: $81 \mathrm{~cm}^{2}$

## Solution 41

Area of Rectangle CDEG $=2 \times 32=64 \mathrm{~cm}^{2}$

Since Rectangle ABGE and Rectangle CDEG have the same length, and $A D$ is thrice of $A E$,

Area of Rectangle $\mathrm{ABGE}=64 \div 2=32 \mathrm{~cm}^{2}$

Area of Triangle EHG $=32 \div 2=16 \mathrm{~cm}^{2}$
Shaded area $=64-32+16=48 \mathrm{~cm}^{2}$

Ans: $48 \mathrm{~cm}^{2}$

## Solution 42



Area of Part P + Area of Part X
= Area of Triangle BEC
$=\frac{1}{2} \times 600=300 \mathrm{~cm}^{2}$

Area of Part Q + Area of Part X
= Area of Triangle BFC
$=\frac{1}{2} \times 600=300 \mathrm{~cm}^{2}$
Area of Part P + Area of Part X

+ Area of Part Q + Area of Part X
$=300+300=600 \mathrm{~cm}^{2}$
$2 \times$ Area of Part X=600-150 $=450 \mathrm{~cm}^{2}$
Area of Part $X=450 \div 2=225 \mathrm{~cm}^{2}$

Ans: $225 \mathrm{~cm}^{2}$

## Solution 43

True:
The line QS can be the height of both Triangle QRS and Triangle PQS.
Reason:
If the height of Triangle QRS is QS, the base is $S R$.
If the height of Triangle PQS is QS, the base is PS.

False:
If the base of Triangle $\operatorname{PQR}$ is $P R$, the height is PQ .
Reason:
If the base of Triangle $P Q R$ is $P R$, the height is QS.

## Solution 44

(a) AC
(b) CF

## Solution 45

False: The area of Triangle ABC is $90 \mathrm{~cm}^{2}$.
Reason:
Area of Triangle ABC $=\frac{1}{2} \times 12 \times 9=54 \mathrm{~cm}^{2}$

False:
When the height and base of Triangle ABC is doubled, the area of the new triangle is also doubled.

Reason:
Area of new triangle $=\frac{1}{2} \times(2 \times 12) \times(2 \times 9)$
$=216 \mathrm{~cm}^{2}$
$\frac{216}{54}=4$
The area of the new triangle is four times the area of Triangle ABC.

## Solution 46

(a) Area of Triangle $\mathrm{ABE}=\frac{1}{2} \times \mathrm{AE} \times \mathrm{BD}$ $=\frac{1}{2} \times E D \times B D=$ Area of Triangle BED $=16 \mathrm{~cm}^{2}$

Ans: $16 \mathrm{~cm}^{2}$
(b) Area of Triangle EBC $=\frac{1}{2} \times E D \times B C$

$$
\begin{aligned}
& =\frac{1}{2} \times \mathrm{ED} \times\left(\frac{1}{2} \times \mathrm{BD}\right)=\frac{1}{2} \times \frac{1}{2} \times \mathrm{BD} \times \mathrm{ED} \\
& =\frac{1}{2} \times \text { Area of Triangle } \mathrm{BED}=\frac{1}{2} \times 16=8 \mathrm{~cm}^{2}
\end{aligned}
$$

Ans: $8 \mathrm{~cm}^{2}$

## Solution 47

Length of rectangle
$=4 \times$ Breadth of rectangle
Breadth of rectangle $=24 \div 8=3 \mathrm{~cm}$

Height of Triangle ACY $=4 \times 3=12 \mathrm{~cm}$

Base of Triangle $\mathrm{ACY}=2 \times 3=6 \mathrm{~cm}$

Area of Triangle ACY $=\frac{1}{2} \times 12 \times 6=36 \mathrm{~cm}^{2}$

Ans: $36 \mathrm{~cm}^{2}$

## Solution 48

Area of Rectangle $\mathrm{ABCD}=(11+9) \times 8$
$=160 \mathrm{~cm}^{2}$

Area of Triangle $P Q C=\frac{1}{2} \times 9 \times 12=54 \mathrm{~cm}^{2}$

Length of $\mathrm{PB}=12-8=4 \mathrm{~cm}$

Length of $\mathrm{SB}=11+9-17=3 \mathrm{~cm}$

Area of Triangle PBS $=\frac{1}{2} \times 4 \times 3=6 \mathrm{~cm}^{2}$

Area of Figure ASPQD $=160+54+6$
$=220 \mathrm{~cm}^{2}$

Ans: $220 \mathrm{~cm}^{2}$

## Solution 49

Area of shaded part $=\frac{1}{8} \times 12 \times 12=18 \mathrm{~cm}^{2}$
Area of Triangle EFG $=\frac{1}{2} \times 35 \times 20=350 \mathrm{~cm}^{2}$

Unshaded area of Triangle EFG $=350-18$ $=332 \mathrm{~cm}^{2}$

Ans: $332 \mathrm{~cm}^{2}$

## Solution 50

(a) Area of Triangle $\mathrm{ABH}=\frac{1}{2} \times \mathrm{AB} \times \mathrm{BH}$
$72=\frac{1}{2} \times \mathrm{AB} \times \mathrm{BH}$
$\mathrm{AB} \times \mathrm{BH}=2 \times 72=144$
$\mathrm{AB}=\mathrm{BH}=\sqrt{144}=12 \mathrm{~cm}$

Length of a side of Square BCDE $=\sqrt{25}$ $=5 \mathrm{~cm}$

Area of Triangle BHE $=\frac{1}{2} \times 12 \times 5=30 \mathrm{~cm}^{2}$
Ans: $30 \mathrm{~cm}^{2}$
(b) Length of a side of Square EFGH $=\sqrt{169}$ $=13 \mathrm{~cm}$

Perimeter of the shaded area
$=(3 \times 13)+(3 \times 5)+12=66 \mathrm{~cm}$

Ans: 66 cm

## Solution 51

Length of $\mathrm{EC}=\frac{1}{3} \times 78=26 \mathrm{~cm}$

Area of Triangle ACE $=\frac{1}{2} \times 26 \times 40=520 \mathrm{~cm}^{2}$

Area of Triangle BCE $=\frac{1}{2} \times 26 \times 40=520 \mathrm{~cm}^{2}$

Area of Triangle $B C F=520-130=390 \mathrm{~cm}^{2}$
Total area of shaded region $=520+390$ $=910 \mathrm{~cm}^{2}$

Ans: $910 \mathrm{~cm}^{2}$

## Solution 52

(a) Length of $\mathrm{AD}=42 \div 2=21 \mathrm{~cm}$

Ans: 21 cm
(b) Length of $\mathrm{AP}=\frac{3}{7} \times 21=9 \mathrm{~cm}$

Length of $\mathrm{PD}=21-9=12 \mathrm{~cm}$

Total area of Triangle APQ and Triangle BSR
$=2 \times \frac{1}{2} \times 9 \times 9=81 \mathrm{~cm}^{2}$
Total area of Triangle PDT and Triangle SCT $=\frac{1}{2} \times 42 \times 12=252 \mathrm{~cm}^{2}$

Area of Rectangle $\mathrm{ABCD}=42 \times 21=882 \mathrm{~cm}^{2}$
Area of the shaded region $=882-81-252$ $=549 \mathrm{~cm}^{2}$

Ans: $549 \mathrm{~cm}^{2}$

## Solution 53

Length of triangle $=7+4=11 \mathrm{~cm}$
Area of Figure $2=4 \times\left(\frac{1}{2} \times 11 \times 4\right)+(7 \times 7)$
$=137 \mathrm{~cm}^{2}$

Ans: $137 \mathrm{~cm}^{2}$

## Solution 54



Area of Triangle $\mathrm{ABX}=\frac{1}{2} \times 9 \times(9+7)$
$=72 \mathrm{~cm}^{2}$

Area of Square $\mathrm{XYDZ}=4 \times 4=16 \mathrm{~cm}^{2}$
Area of Triangle CYD $=\frac{1}{2} \times 4 \times(9+4)$
$=26 \mathrm{~cm}^{2}$

Shaded area $=72+16-26=62 \mathrm{~cm}^{2}$

Ans: $62 \mathrm{~cm}^{2}$

